# An overview of methods for treating selectivity in big data sources

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Presentation is partially based on:

- Beręsewicz, Lehtonen, Reis, Di Consiglio and Karlberg (2018), An overview of methods for treating selectivity in big data sources, published in Eurostat's Working Papers – part of the ESSnet on Big Data project.
- NCN Preludium 7 grant no. 2014/13/N/HS4/02999.

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#### Introduction

## An overview of methods for treating selectivity in big data sources

MACIEJ BERĘSEWICZ, RISTO LEHTONEN, FERNANDO REIS, LOREDANA DI CONSIGLIO, MARTIN KARLBERG

#### 2018 edition



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#### Motivation - new data sources for statistics

- Increasing unit non-response in sample surveys;
- Growing information needs at a low level of (spatial) aggregation;
- A change of paradigm in official statistics, which involves the adoption / reuse of existing data sources instead of creating new ones (cf. ESSnet on Big Data);
- Internet data sources (IDSs) and big data are still not recognized and their *suitability as statistical sources is often unknown*;
- New data sources, in particular big data and the Internet have become an important issue in official statistics and small area estimation (cf. Daas et al., 2015; Japec et al., 2015; Pfeffermann et al., 2015, Marchetti et al., 2015; Schmid et al., 2017).
- Note that, The Internet, moreover, not only generates a great deal of today's "big data", but also provides ordinary-size data in a more accessible way – for example, access to public opinion polls or to local property records (Citro, 2014).

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What is big data?			

### What is big data?

Happy families are all alike; every unhappy family is unhappy in its own way

Leo Tolstoy

...tidy datasets are all alike but every messy dataset is messy in its own way

Hadley Wickham (JSS, 2014)

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## What is big data?



Figure 1: Example base transceiver station (BTS) from with several antennas located close by this Faculty

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> orange	e_bts	naver id	mohi	le number 2		tart date	length	cost	service id loca	tion bts i	id.
1:	f631585c5cdfcdcc44f54764a87cfa43	8636554	c215a10de85fc75d12183	f45a133d524	2013-01-15	12:00:02	Ø	2.0	6	1972	0
2:	a95c35c1b6457e0ce1070a6b8bb36c08	9165023	8944cba2bafe6c7b943cf	31866cda1b3	2013-01-15	12:00:13	0	2.0	6	1972	20
3:	c3244b0c788736657d89bd03e355f854	7862577	c215a10de85fc75d12183	f45a133d524	2013-01-15	12:00:25	0	2.0	6	1972	20
4:	70e617965a33700fba187bc275e4b992	1889161	4f4302b958d33ee33b137	c0c13b046b6	2013-01-15	12:00:19	0	2.0	6	1972	20
5:	0490b8101b50f29f695ae764ea31ba04	4356384	4f4302b958d33ee33b137	c0c13b046b6	2013-01-15	12:00:27	0	2.0	6	1972	20
700855:	5117d5b1f3ae453f01c4353e28279ea1	2752745	3df913615ac1fdca408e8	fa310eaa44d	2013-01-15	12:04:32	67	0.0	3001	500	91
700856:	4197cf577efcbce7d7903808e81f8a1a	9142277	1203e523b3cbd175413c6	5bcd06391d7	2013-01-15	12:13:56	88	0.0	3001	500	91
700857:	2215fd79744d43974bd304b9dbfff77e	2752745	3df013615ac1fdca/08e8	fp310epp///d	2013-01-15	12.14.30	31	0 0	3001	500	1

23 0.1

3001

1282

5001

Figure 2: Example records from Call Details Records (CDR) data (contracts only)

blackberry.net 2013-01-15 12:02:33

bc9fad9899c25 8527717 120adb4955ae23fc5febcfd00d

Two type of mobile phone data (in most cases there is no link with CRM systems):

- active (CDR) needs an action e.g. call, sms, internet connection (39 mln actions on one day) – pseudo-response.
- passive (signalling data) no actions needed, e.g. switching between antennas, signal strength unaware response?

#### What are the implications?

700859: 499c9c853c5e5e40956de07385937cc7 10002961

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## What is big data?



Figure 3: Number of active users in Poland based on CDR data (contracts only). Number of Polish citizens 15+32,7 mln

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Table 1: Selected characteristics of user's activities between 1st February and 31th May

User ID	# contacts	<b>#</b> sms	# calls	calls duration	∦ bts	# days
891026	2549	4	12	0.28	2	27
1958650	683	-	454	4.24	7	74
4009251	461	-	302	7.25	4	81
3086158	460	_	305	7.22	5	81
4632841	460	-	300	7.13	5	81

Note: # contacts – daily average number of unique contacts, sms – daily median number of send sms, calls – daily median number of calls made, calls duration – daily average calls duration (in hours), # bts – number of unique bts, # day – number of days with activity (max 81).

**Signalling data do not allow to calculate such statistics**, thus may be harder to remove units that do not belong to the population of interest.

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	Pielęgniarka Nowa Dom Pomocy spolecznej	Ŕ
	Białystok, PL	
	🗇 Opublikowana mniej niż godzinę temu	
	() Bądź jednym z pierwszych 10 aplikujących.	
	Aplikuj w witrynie firmy	
Opis oferty pracy	Firma	
Opis stanow	iska	Branża
sprawowanie be przedlekarskiej	zpośredniej opieki nad mieszkańcami, udzialanie pomocy w stanach zagrożenia życia oraz przy urazach, zranieniach,	Szpitale i opieka zdrowotna
oparzeniach, sk	adanie sprawozdania o stanie zdrowia podopiecznych, ich	Forma zatrudnienia
zacnowaniu, po konsultacji w po	dawanie lekow , towarzyszenie mieszkańcom podczas iradniach specjalistycznych	Pełny etat
		Doświadczenie
		Partner
		Obowiązki służbowe
		Opieki zdrowotna

Figure 4: Example job offer from Linkedin seen from the web browser

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#### What is big data?

```
"decoratedJobPostingsModule": {
    "elements": [
           "isInApply": false.
           "decoratedJobPosting": {
               "iobPostina": {
                   "listDate": 1534860416000,
                   "countryCode": "pl",
                   "companyName": "Dom Pomocy Społecznej w Białymstoku",
                   "listingType": "BASIC",
                   "id": 816002536,
                   "applicationRouting" "COMPANY_WEBSITE".
                   "sourceDomain": "oferty.praca.gov.pl",
                   "title": "Pielegniarka"
               }.
               "formattedDescription": "Sprawowanie bezpośredniej opieki nad mieszkańcami, udzialanie
                   pomocy przedlekarskiej w stanach zagrożenia życia oraz przy urazach, zranieniach,
                   oparzeniach, skladanie ...",
               "formattedTitle": "",
               "cityState": "Białystok, PL",
               "companyName": "Dom Pomocy Społecznej w Białymstoku",
               "formattedLocation": "Białystok, PL",
               "decoratedCompany": {
                   "company": {
                       "companyId": 8069002,
                       "names": [
                               "name": "DOM POMOCY SPOLECZNEJ".
                               "active": true.
                               "locale": "en US".
                               "type" "CANONICAL"
                       1,
                       "universalName": "dom-pomocy-spolecznei"
                   },
                   "hasPaidLcp": false.
                   "canonicalName": "DOM POMOCY SPOLECZNEJ"
               }.
```

Figure 5: Example job offer from Linkedin seen from a different perspective

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# How new are big data for statistics?

#### Non-statistical definitions of big data

Big data are highly detailed exhaust data automatically captured by sensors or generated during the use of IT systems.

#### Big data in statistics (survey methodology)

- an imperfect frame(s),
- non-probability character (cf. non-probability samples),
- creation mechanism involves a self-selection process (cf. non-response in surveys; opt-in panels),
- paradata-designed to capture the process and all possible data (cf. paradata in survey data collection).

## How new are big data for statistics? - Big data survey

#### Big data survey – why?

- another type of secondary data source (collected for other purposes; cf. register-based surveys),
- a new kind of Internet survey (automated data collection made via the Internet and IoT),
- an opt-in panel (non-probability selection, longitudinal observation and data collection).

#### Possible ways of using big data

We can distinguish the following ways of using big data for statistics

- as auxiliary variables cf. Marchetti et al. (2015), van den Brakel et al. (2017) – question: is this effort worth it?
- as extension to existing sources e.g. demand for labour survey + online job vacancies (e.g. Beręsewicz et. al (2018b)).
- as main source for statistics e.g. road statistics in the Netherlands.

## How new are big data for statistics? - selectivity

 $(\dots)$  selectivity as a general term for selection errors resulting from:

- (self-selection) decisions of individuals (e.g. whether to tweet or use a particular mobile provider),
- decisions of the owners of the electronic platforms where data are captured (e.g. in terms of business concept, technical infrastructure), or
- the limitations of the technologies.

As a result, selectivity causes coverage, measurement and non-response (or missingness) errors, which introduce potential bias in estimates based on big data sources.

Not an easy task to distinguish from coverage and (non-response) selection bias.

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Quality issues			

Statistica Neerlandica (2012) Vol. 66, nr. 1, pp. 41-63 doi:10.1111/j.1467-9574.2011.00508.x

# Topics of statistical theory for register-based statistics and data integration

Li-Chun Zhang\*

Statistics Norway, Kongensgt. 6 Pb 8131 Dep, N-0033 Oslo, Norway

Journal of Official Statistics, Vol. 33, No. 2, 2017, pp. 477-511, http://dx.doi.org/10.1515/JOS-2017-0023

#### Extending TSE to Administrative Data: A Quality Framework and Case Studies from Stats NZ

Giles Reid<sup>1</sup>, Felipa Zabala<sup>2</sup>, and Anders Holmberg<sup>3</sup>

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Missing data mechanisms

#### Missing data mechanisms

Biometrika (1976), 63, 3, pp. 581–92 Printed in Great Britain

#### Inference and missing data

By DONALD B. RUBIN

Educational Testing Service, Princeton, New Jersey

#### SUMMARY

When making sampling distribution inferences about the parameter of the data,  $\theta$ , it is appropriate to ignore the process that causes missing data if the missing data are 'missing at random' and the observed data are 'observed at random', but these inferences are generally conditional on the observed pattern of missing data. When making directlikelihood or Bayesian inferences about  $\theta$ , it is appropriate to ignore the process that causes missing data if the missing data are missing at random and the parameter of the missing data process is 'distinct' from  $\theta$ . These conditions are the weakest general conditions under which ignoring the process that causes missing data always leads to correct inferences.

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## Missing data mechanisms

Some notation

- U the target population,  $U_I$  is the Internet population,  $U_{NI}$  is the non-Internet population (in practice more complicated; cf. Zhang 2012, Beręsewicz et al. 2018a, ch. 3).
- N size of the target population, k = 1, ..., N,
- Y target variable (e.g. number of job vacancies, support for given party); Y<sub>obs</sub> observed data, Y<sub>mis</sub> not observed (missed) data,
- $I_k \in \{0, 1\}$  an indicator variable; if given unit from U has access to the Internet;  $\sum_k (I_k = 1) = N_I$ ,  $\sum_k (I_k = 0) = N_{NI}$
- *R<sub>k</sub>* ∈ {0,1} an indicator variable; if given unit from *U* or *U<sub>l</sub>* participate in survey, study, or use given social media, or provide information on social media (e.g. tweet). This variable might be used to generally define any interaction with the Internet / IoT.
- $\rho_k = E(R_k)$  the **response probability** of element *k*.

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Rubin (1976) proposed the following classification of missing data mechanisms (we drop  $I_k$  for simplicity):

- Ignorable:
  - Missing Completely at Random (MCAR)

$$Pr(R=1|Y_{obs},Y_{mis},\psi)=Pr(R=1|\psi)=const.$$
 (1)

• Missing at Random (MAR) - depends solely on the observed data

$$Pr(R = 1|Y_{obs}, Y_{mis}, \psi) = Pr(R = 1|Y_{obs}, \psi).$$
(2)

- Non-ignorable:
  - Not missing at random (NMAR) depends both on the observed and non-observed data

$$Pr(R = 1 | Y_{obs}, Y_{mis}, \psi).$$
(3)

Real life issue - Swiss cheese data (full of item non-responses).

Summary

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#### How to correct selection bias ?

Econometrica, Vol. 47, No. 1 (January, 1979)

#### SAMPLE SELECTION BIAS AS A SPECIFICATION ERROR

#### By James J. Heckman<sup>1</sup>

This paper discusses the bias that results from using nonrandomly selected samples to estimate behavioral relationships as an ordinary specification error or "omitted variables" bias. A simple consistent two stage estimator is considered that enables analysts to utilize simple regression methods to estimate behavioral functions by least squares methods. The asymptotic distribution of the estimator is derived.

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#### How to correct selection bias ?

Statistical Science 2017, Vol. 32, No. 2, 249–264 DOI: 10.1214/16-STS598 © Institute of Mathematical Statistics, 2017

#### Inference for Nonprobability Samples

#### Michael R. Elliott and Richard Valliant

Abstract. Although selecting a probability sample has been the standard for decades when making inferences from a sample to a finite population, incentives are increasing to use nonprobability samples. In a world of "big data", large amounts of data are available that are faster and easier to collect than are probability samples. Design-based inference, in which the distribution for inference is generated by the random mechanism used by the sampler, cannot be used for nonprobability samples. One alternative is quasi-randomization in which pseudo-inclusion probabilities are estimated based on covariates available for samples and nonsample units. Another is superpopulation modeling for the analytic variables collected on the sample units in which the model is used to predict values for the nonsample units. We discuss the pros and cons of each approach.

Key words and phrases: Coverage error, hierarchical regression, quasirandomization, reference sample, selection bias, superpopulation model.

So, how we can correct the bias due to self-selection character of big data source?

In the statistical literature, we can find two approaches:

- Quasi-randomization approach where we somehow weight our sample to known population totals, including modelling propensity to respond.
- **Prediction / superpopulation model approach** where we build a model on a sample and then predict for out-of-sample units.
- ... and a mix of these two.

However, there is one general statistically sound (always working) method, nor established methodology that removes 100% of bias due to non-response.

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#### How to correct selection bias ?

	Low Association $(X, Y)$	High Association $(X, Y)$
Low association (X,R)	Little effect on bias;	Little effect on bias;
	Little effect on variance	Variance reduction
High association $(X,R)$	Little effect on bias;	Bias reduction;
	Variance inflation	Variance reduction

Figure 6: Effect of bias correction method; Zhang, Thomsen and Kleven (2013)

All approaches requires **Y** or/and **X**, **Z** (auxiliary, proxy) to be present in data source and some known / estimated population totals/means/quantiles...

...but do we have (good) population totals or even defined population (e.g. day-night population, job vacancies)?

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#### How to correct selection bias ?

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Quasi-randomization approach

## How to estimate propensities or to reweight?

In the literature we can find the following approaches:

- **Reference survey**. One approach is to use a reference survey in parallel to the non-probability survey / big data. The underlying idea is to:
  - combine the reference sample and the sample of volunteers and fit a model to predict the probability of being in the non-probability sample / big data.
- **Sample matching** be done on an individual or aggregate level
  - individual-level matching matching cases from non-probability sample / big data to probability sample – e.g. using propensity scores (Rosenbaum and Rubin 1983)
  - aggregate level consists making the frequency distribution of the non-probability sample / big data the same as that of the population - e.g. using post-stratification, calibration (cf. Devill and Särndal, 1992)).

Summarv

Quasi-randomization approach

#### Quasi-randomization approach

Ideally, we would like to construct weights that capture:

- Undercoverage error (denote by  $c_k$ )
- Different propensities to respond (denote by  $\rho_k$ )
- Differences in distributions of socio-demografic variables (denote by  $d_k$ )

In the end we are interested in some quantity, say, total:

$$\hat{Y} = \sum_{k} d_k \rho_k^{-1} c_k^{-1} y_i.$$
(4)

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Calibration			

- This technique was proposed by Devill and Särndal (1992) and is a method of searching for so called calibrated weights by minimizing distance measure between the sampling weights and the new weights, which satisfy certain calibration constraints.
- As a consequence when the new weights are applied to the auxiliary variables in the sample, they reproduce the known population totals of the auxiliary variables exactly.
- It is also important that the new weights should be as close as possible to sampling weights in sense of chosen distance measure (Särndal C-E., Lundström S. 2005, Särndal C-E. 2007).
- In case of big data the sampling weights can be replaced by either pseudo-weights equal to one or N/n.

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#### Quasi-randomization approach

## Calibration - how to find weights

(C1) Find the minimum of distance function:

$$D(\mathbf{w}, \mathbf{d}) = \frac{1}{2} \sum_{i=1}^{n} \frac{\left(w_i - d_i\right)^2}{d_i} \longrightarrow \min,$$
(5)

(C2) Calibration equations:

$$\sum_{i=1}^{n} w_i x_{ij} = \mathbf{X}_j, \quad j = 1, \dots, k,$$
(6)

(C3) Calibration constraints:

$$L \leq \frac{w_i}{d_i} \leq U$$
, where:  $L < 1$  i  $U > 1$ ,  $i = 1, \dots, n$ . (7)

Can be easily done in R with survey::calibrate, sampling::calib or laeken::calibWeights.

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#### Alternative approach – no auxiliary variables

Recently, Matei and Renalli (2015) suggested using latent trait models (item response theory) to deal with non-ignorable item non-response, i.e. missing data depends on the study variable itself. This is also known as missing not at random (MNAR) mechanism.

The proposed approach assumes that there is an underlying latent variable that drives respondents to answer questions.

The approach has two steps:

OOO Quas

- modelling non-response based on item non-response in order to estimate probability to respond to survey denoted by *p<sub>i</sub>*,
- modelling item non-response to estimate probability to respond to given question denoted by q<sub>ik</sub>

In the presentation we focus on the first part i.e. modelling probability to respond denoted by  $p_i$ .

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#### Alternative approach – no auxiliary variables

Let assume that there is a latent variable  $\theta_i$  denoting 'willing to respond' by unit *i*. Assuming that  $\theta_i$  is known for all units in *U*, in absence of auxiliary variables we can estimate  $\theta_i$  and thus,  $p_i$  by

$$p_i = \Pr(R_i = 1 | \theta_i) = \frac{1}{1 + \exp(-\alpha_0 - \alpha_1 \theta_i)}.$$
(8)

Matei and Renalli (2015) proposed to estimate  $p_i$  in two steps:

- estimate θ<sub>i</sub> using latent trait model based on non-response patterns created by item non-response,
- estimate  $p_i$  based on logistic regression using estimated  $\hat{\theta}_i$  as a covariate.

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## Matei and Renalli (2015) estimator

Matei and Renalli (2015) proposed the following estimator of total:

$$\hat{Y} = \sum_{i} \frac{y_{ik}}{\pi_i p_i q_{ik}},\tag{9}$$

where *i* denotes respondent, *k* denotes given question,  $\pi_i$  is the inclusion probability,  $p_i$  is the estimated propensity to respond,  $q_{ik}$  is the probability to respond to question *k*.

Note: Tested on small (<500) data, with bigger data calculation of  $p_i$  or  $q_{ik}$  might be problematic (near zero).

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#### Prediction / superpopulation model approach

#### Prediction / superpopulation model approach

The general framework is as follows:

• We assume that model build on a sample holds for the population:

$$f_{s}(y_{k}|x_{k}) = \frac{Pr(R_{i} = 1|x_{i}, y_{i})f_{P}(y_{i}|x_{i})}{Pr(R_{i} = 1|x_{i})}.$$
 (10)

We do not assume any form of the model (e.g. machine learning could be used).

• Then we predict for the non-sampled units

$$\hat{y} = \sum_{k \in s} y_k + \sum_{k \notin s} \hat{y}_k.$$
(11)

Recently: LASSO regression for non-probability samples (Chen, 2016; Chen, Valliant and Elliott 2018), other types of model-calibration / modelassisted estimators (see Statistical Science) or multilevel regression and post-stratification (see Andrew Gelman works).

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#### Sample selection models – Heckman

The basic idea is as follows, we model jointly selection (S) and outcome (O) equation, given by

$$y_i^{S*} = \boldsymbol{\beta}^{S'} \boldsymbol{x}_i^{S} + \varepsilon_i^{S}$$
$$y_i^{O*} = \boldsymbol{\beta}^{O'} \boldsymbol{x}_i^{O} + \varepsilon_i^{O}$$

where errors are correlated assuming normal distribution

$$\left(\begin{array}{c} \epsilon^{S} \\ \epsilon^{O} \end{array}\right) \sim N\left(\left(\begin{array}{c} 0 \\ 0 \end{array}\right), \left(\begin{array}{c} 1 & \rho \\ \rho & \sigma^{2} \end{array}\right)\right)$$

then

$$y_i^{O} = \boldsymbol{\beta}^{O'} \boldsymbol{x}_i^{O} + \mathrm{E}\left[\boldsymbol{\varepsilon}^{O} | \boldsymbol{\varepsilon}^{S} \geq -\boldsymbol{\beta}^{S'} \boldsymbol{x}_i^{S}\right] + \eta_i \equiv \boldsymbol{\beta}^{O'} \boldsymbol{x}_i^{O} + \rho \sigma \lambda \left(\boldsymbol{\beta}^{S'} \boldsymbol{x}_i^{S}\right) + \eta_i.$$

Sample selection models

## Sample selection models – Heckman and others

- Joint modelling selection mechanism and Y variable,
- Requires X to formulate a model,
- Basic model works only for normally distributed data and probit link,
- Extensions and packages:
  - SampleSelection binary and continuous,
  - SemiParSampleSel binary, count and Continuous with copulas,
  - miceMNAR multiple imputation based on Heckman's selection model for binary and continuous variables.
  - GJRM Generalised Joint Regression Modelling the most comprehensive software.

Other approaches: see Pfefferman & Sverchkov works, Sikov (2018), Riddles et al. (2016). How to correct selection bias ?

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#### Online job vacancies – auxiliary variables

Table 2: Quality of coding measured by number of job offers with digits based on pooled data from 2011, 2013 and 2014 for occupation (max 6 digits) and 2011-2014 for NACE (max 3 digits)

Number of digits	Occupancy	NACE
6 digits	1 693	-
5 digits	53 533	-
4 digits	5 311	-
3 digits	799	30 934
2 digits	313	15 609
1 digits	1	7 610

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#### Online job vacancies – target variables

Table 3: Share of competences included in job offers by data source based on pooled data 2011, 2013 and 2014

Competences	Online data	District Labour Offices
Artistic	15.99	2.25
Availability	20.86	2.74
Cognitive	20.28	1.57
Computer	32.03	8.52
Interpersonal	54.34	6.84
Managerial	26.04	1.74
Mathematical	0.37	0.06
Office	3.82	1.72
Physical	5.29	1.85
Self-organization	59.08	7.80
Technical	4.27	5.02

Source: Beręsewicz et al. (2018).

Summary

References

Sample selection models

#### Online job vacancies – auxiliary variables

Table 4: Cramer's V between competences and occupation, NACE and voivodeship based on the pooled data for 2011, 2013 and 2014

Competences	Occupation	NACE	Voivodeship
Artistic	0.24	0.11	0.08
Availability	0.19	0.10	0.05
Cognitive	0.27	0.16	0.10
Computer	0.47	0.21	0.13
Interpersonal	0.50	0.33	0.11
Managerial	0.37	0.19	0.06
Mathematical	0.05	0.04	0.03
Office	0.14	0.07	0.04
Physical	0.11	0.06	0.04
Self-organization	0.44	0.29	0.12
Technical	0.23	0.10	0.06

Sample selection models

#### Online job vacancies – share of selected competences

Table 5: Share of selected competences in 2014 based on three estimators and online data

Competence	Naive	Calibrated	Heckman
Interpersonal	61%	45%	55%
Technical	4%	7%	14%
Managerial	31%	23 %	29%

*Naive* – simple average; *Calibrated* – adjusted for occupancy totals; *Heckman* – selection model based on occupancy and voivodeship, outcome model based solely on occupancy, based on multiple imputation with miceM-NAR. Population totals – estimates from the Demand of Labour survey.

## Summary

- Strong auxiliary variables are needed need to be extracted, if any exist.
- Population level information is required definition of population? do we actually have these information or some proxy?
- One should consider that in big data NMAR is more common than MAR however methods that account for this type of error are quite complex consider bias exploration, if possible (cf. Zhang 1999).

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Summary

#### Conclusion

Inference from probability samples are all alike but inference from messy non-probability sample (big data) is messy in its own way.

Are we actually prepared for big data?

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Summary

## Conclusion

Inference from probability samples are all alike but inference from messy non-probability sample (big data) is messy in its own way.

Are we actually prepared for big data?

Summary

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# Thank you!